PETROPHYSICS

Physical properties of natural stone and other porous mineral materials

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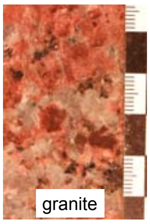
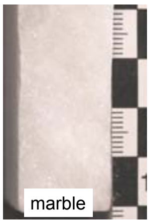
Depending on the use (cobblestone, stair, façade, carved element, pile of bridge…), stone must have different physical characteristics.

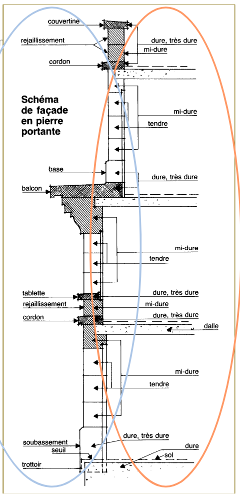
The physical properties of stones depend on cementation, porosity…





☛ they depend on **the origin of stones**

Architectural elements of a façade



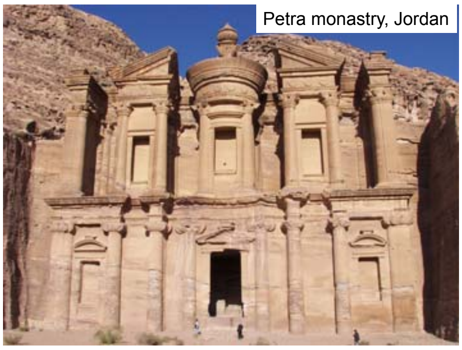
Stones qualities:

Très dure: very hard
Dure: hard
mi-dure: half-hard
tendre: soft

In the same exposure conditions, the durability of stones lying side by side depends on the liquids and gaseous exchanges between them and their environment (=physical properties)


Lausanne, Cathedral, 10.04.2012

Exchanges between stones and the environment depend on:
- the **quantity** of the **pore space**
- the **quality** of the **pore space** (geometry of pores, mineralogical nature of the inner surfaces…)

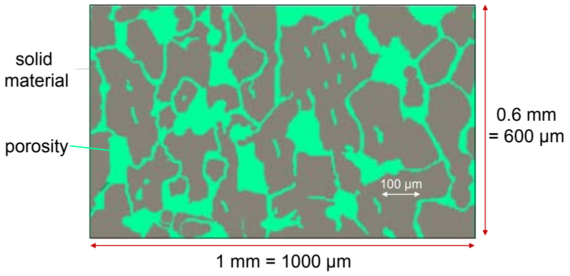

Petra monastry, Jordan

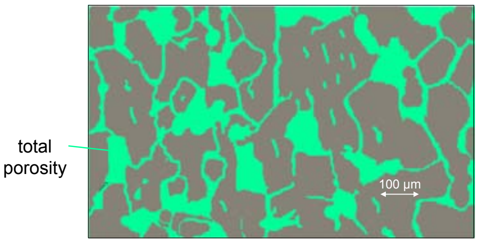
Interactions between stones and conservation products are also strongly dependent on quantity and quality of the porous space

Conservation products for stones*, mechanical and/or chemical cleanings -as well as water and salts- can change the physical properties of stones

* (consolidants, water-repellents, anti-graffiti products, paints, …)

Porosity





(Total) porosity

Definition: fraction of the total volume of a material « occupied » by voids

$$\mathbf{Pt\ (\%) = 100 \times \frac{Vv}{Vt} = 100 \times \frac{Vv}{Vv + Vs}}$$

Pt = total porosity
Vv = volume of the voids
Vt = bulk volume
Vs = volume of solid

Densities and porosity

Density (masse volumique): quantity of solid matter contained in a given volume of material

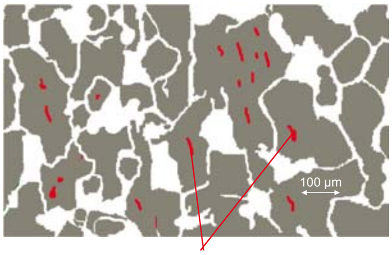
bulk density $\rho_a = \frac{m}{Vt}$
(m. vol. apparente)

particle or true density $\rho_s = \frac{m}{Vs}$
(m. vol. réelle ou solide)

$$\mathbf{Pt\ (\%) = 100 \times \left(1 - \frac{\rho_a}{\rho_s}\right)}$$

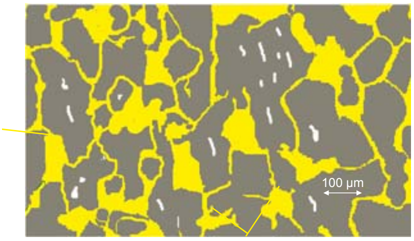
If Pt tends to 0, ρ_a tends to ρ_s

Different kinds of porosity



occluded porosity

Different kinds of porosity



connected porosity

Different kinds of porosity

- **Connected**: voids communicating freely between them
- **Occluded**: not inter-connected voids
- **Primary** **(primaire)**: structural arrangement existing since the genesis of the stone
- **Secondary** **(secondaire)**: results from the phenomena of deterioration, diagenesis, metamorphism …
- **Intergranular**: voids between the constituent grains
- **Intragranular**: voids inside the constituent grains
- **Micro- and macro- porosity** : < or > to 7.5 µm (from mercury injection porosimetry : injection PHg = 1 bar)

Different kinds of porosity

Porosity and water retention in soils

Pores	diameter	Water
Big pores	> 50 µm	free water - dry quickly and easily (no capillary action)
Medium pores	10 to 50 µm	free/capillary water - take time to the dry out ("coarser" part of the capillary porosity)
Fine pores	0.2 to 10 µm	capillary water - slow to dry, high capillary tension
Very fine pores	< 0.2 µm	linked (adsorbed) water - very difficult/impossible to dry

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Total porosity ranges for various natural rocks

Rock type	Porosity *(%)*
sandstones	5 – 50
limestones	5 - 55
crystalline rocks	0 – (10)
volcanic rocks	0 – (90)
metamorphic rocks	0 – (50)

Sources: Freeze and Cherry (1979); McWorter and Sunada (1977).

Total porosity ranges for various natural swiss rocks

PIERRES NATURELLES	Masse volumique apparente	Résistance à la compression	Résistance à la flexion	Porosité totale (connectée)	Porosité capillaire	Dilatation hydrique
	t/m³	N/mm²	N/mm²	Vol.%	Vol.%	mm/m
R. MAGMATIQUES						
Plutoniques	2.6-3.0	80-300	10-40	0.4-1.5	0.2-1.2	0.06-0.2
Volcaniques effusives	1.6-3.1	10-400	5-60	0.2-30	0.1-25	0.06-0.4
R. SEDIMENTAIRES						
Calcaire/ dolomite dures	2.6-2.8	50-200	3-30	0.6-2	0.5-1.5	0.09-0.16
Travertin / tuf calcaire	1.7-2.5	10-80	3-20	2-25	1.5-20	
Calcaire tendre	1.5-2	8-25	2-8	5-25	5-20	0.3-0.5
Grès à ciment siliceux	2-2.6	40-250	7-33	1-25	1-20	0.3-0.6
Grès à ciment calcaire	2-2.6	30-180	3-18	2-20	1-18	0.4-0.8
Conglomérats	2.4-2.6	14-160	2-12	0.5-5	0.5-4	0.1-0.2
R. METAMORPHIQUES						
Gneiss / migmatite	2.5-2.8	70-200	8-45	0.4-2.0	0.25-1.5	
Quarzite	2.6-2.7	100-300	14-60	0.4-2.0	0.2-1.5	
Schistes	2.5-2.7	50-150	8-40	0.6-3.0	0.5-2.5	0.2-0.6
Serpentinite	2.6-2.75	55-200	11-60	0.3-2.0	0.25-0.18	
Marbre	2.5-2.7	40-230	10-40	0.3-0.8	0.2-0.5	

D'après Kündig R. et al., 1997. Die mineralischen Rohstoffe der Schweiz.
Commission Géotechnique Suisse, Zürich, ETHZ

(connected) Porosity measurement

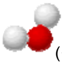
The « triple weighing* » method: (method of imbibition)

M_1 = mass of the dried sample weighing in the air
M_2 = m. of the water saturated s.**, weighing in the air
M_3 = m. of the water saturated s.**, weighing underwater

$M_1 = (\rho_s \text{ x } Vs)$
$M_2 = (\rho_s \text{ x } Vs) + (\rho_{H2O} \text{ x } Vv)$
$M_3 = (\rho_s \text{ x } Vs) - (\rho_{H2O} \text{ x } Vs)$
avec $\rho_{H2O} = 1 \text{ g/cm}^3$

$$\mathbf{Pt} = \frac{\mathbf{M_2 - M_1}}{\mathbf{M_2 - M_3}}$$

☟ water soluble phases !!!



Ø of the H_2O molecule
~0.343 nm
(☟ big pores are not accessible)

*méthode de la triple pesée
** the connected porosity of samples are saturated with water under vaccum

(connected) Porosity measurement

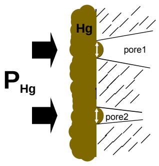
Mercury intrusion porosimetry (MIP): (method of drainage)
The technique involves the intrusion of mercury, a non-wetting liquid, at high pressure into a material through the use of a porosimeter. The pore size can be determined based on the external pressure needed to force the liquid into a pore against the opposing force of the liquid's surface tension (at 25° C γ = 0,474 N/m and the contact angle α = 130°)

$$\mathbf{P_{Hg} - P_{vap}} = \frac{\mathbf{2\gamma \cos\alpha}}{\mathbf{R}} \qquad \textbf{as } \mathbf{P_{vap} << P_{Hg} => P_{Hg}} = \frac{\mathbf{2\gamma \cos\alpha}}{\mathbf{R}}$$

☟ deformable materials ?

● Ø of the Hg atom 0.3 nm
BUT the Ø of the smallest accessible pores depends on the max. PHg (and the largest ones depends on the min. PHg

(connected) Porosity measurement

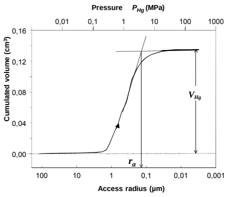


MIP:
With a known **P_{Hg}** on a known volume of mercury, all the pores with an access radius ≥ **R** can be filled

As **P_{Hg}** ↗, the radius **R** of the pores that can be filled ↘

V_{Hg} = bulk volume of intruded mercury (≈ Pt)

ra = threshold radius (the smallest radius giving access to the maximum porous volume)



Sound velocity, porosity and cementation

The time of transmission of the P waves (longitudinal) through the thickness of a porous material ↗ when:
- the percentage of the void volume ↗
- the cementation degree ↘

The Hooke's law (very) simplified allows to estimate the modulus of elasticity or Young's modulus (E):

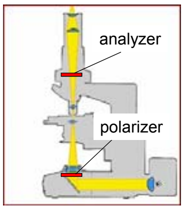
$$Vp = \sqrt{\frac{E}{\rho_a}}$$ **=> relative value**

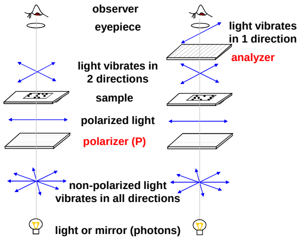
Microscopic observation of thin sections of rocks (polarizing petrographic microscopy)

A thin section ***(lame mince)*** is a 30 µm thick strip of stone which is sticked on a glass slide. This sample can be observed with transmitted light because of its transparency.

Stages of manufacture:
- sawing a stone to « suger cube » (3 x 2 cm) size
- hardening using an epoxy resin
- polishing of one side which is then glued on the glass slide
- sawing, grinding, then polishing up to a thickness of 30 µm

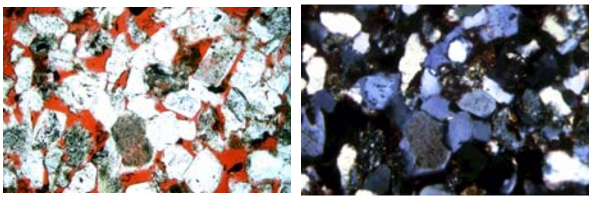
The polarizing petrographic microscope





The optical properties of the minerals in a thin section alter the colour and intensity of the observed light. Minerals can be identified but porosity can also be observed

Microscopic observation of thin sections of rocks



(Photos: D. Jeannette) Sandstone of the Basel cathedrale. Width ≈ 5 mm

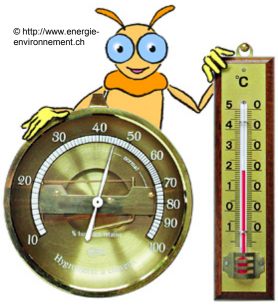
⇒ mineralogy
⇒ geometry of the porous network (only for voids >1 μm)

Notion of climate:

In french
http://c2rmf.fr/sites/c2rmf.fr/files/quest-ce_que_le_climat.pdf
(29.10.2015)

http://www.kasuku.ch/pdf/hygrometrie.pdf
jusqu'à la page 9
(29.10.2015)

In English
http://www.conservationphysics.org/intro/fundamentals.php
(29.10.2015)



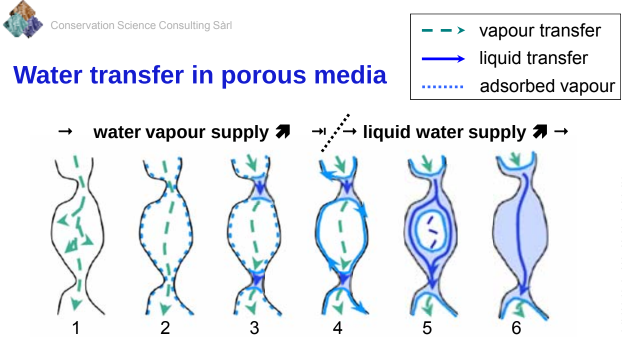
© http://www.energie-environnement.ch

Température

Humidité
(relative et absolue)

Point de rosée

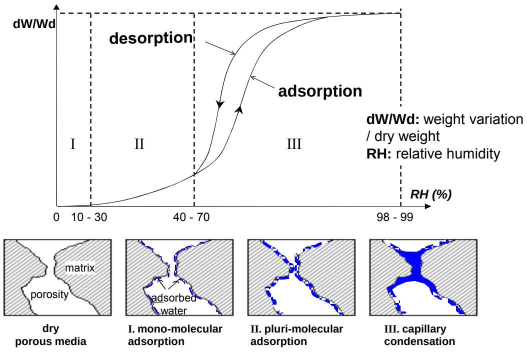
Water transfer in porous media



1 - vapour diffusion; 2 – vapour adsorption + diffusion; 3 - capillary condensation; 4 - capillary migration along the walls (beginning of filling); 5 - hydraulic flow in unsaturated media (filling in progression or finished); 6 - hydraulic flow in saturated media

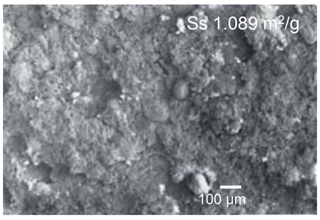
According to Rose (1963)

Water vapour in porous media: adsorption

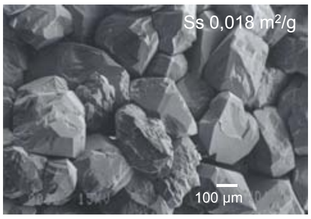


dW/Wd: weight variation / dry weight
RH: relative humidity

Water vapour in porous media: adsorption



Lourdines micrite MCL



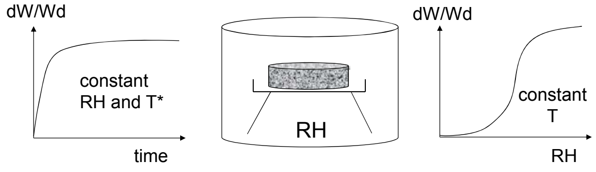
Fontainebleau sandstone GFT

Hygroscopicity increases when:

- specific surface ➚ (microporosity, content of clays – for example MCL hygroscopicity > GFT one)
- content of soluble salts ➚

Water vapour in porous media: adsorption

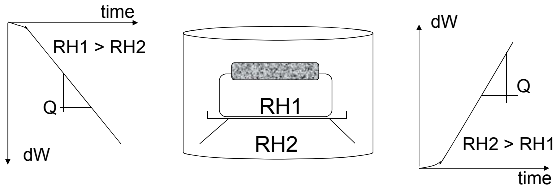
To determine the kinetic adsorption and the adsorption isotherm, samples are first dried at 60ºC then, they are placed in closed boxes where relative humidity is controlled. Then, they are weighted regularly until their mass becomes constant.



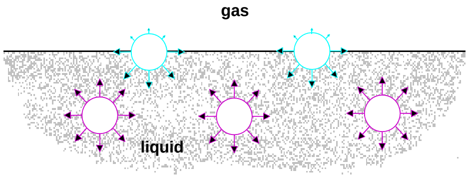
*T = temperature

Water vapour in porous media: permeability

To determine the water vapour diffusivity or the permeability to water vapour samples are first dried at 60ºC. Then they are packed in such a way that two opposite faces can exchange with two different relative humidities.

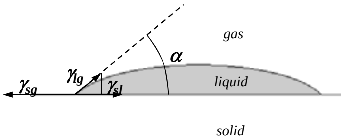


Liquid water in porous media – surface tension



The cause of surface tension in a liquid: a molecule in contact with a neighbour is in a lower state of energy than if it weren't in contact with a neighbour. The boundary molecules have fewer neighbours than interior molecules and are therefore in a higher state of energy than interior molecules => to minimize its energy state, a liquid must minimize its number of boundary molecules and therefore minimize its surface area => formation of "film" => formation of a drop **…**

Liquid water in porous media – surface tension



γ_{sg}	**surface tension solid/gas**
γ_{lg}	**surface tension liquid/gas**
γ_{sl}	**surface tension solid/liquid**
α	**contact angle solid/liquid**

When a drop of liquid is deposited on a solid surface, the interface geometry depends on the affinity of each phase (solid, liquid, gas) to the other, or on their relative surface tensions

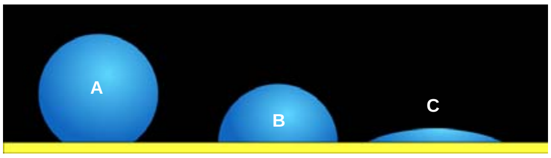
Young-Dupré equation:

$$\gamma_{lg} \cos\alpha = \gamma_{sg} - \gamma_{sl}$$

wetting liquid: $\alpha < 90°$

non-wetting liquid: $\alpha > 90°$

Liquid water in porous media – surface tension



Wetting of different fluids. ***A*** shows a fluid with very **high surface tension** (and thus little wetting), while ***C*** shows a fluid with **very low surface tension** (more wetting action.) A has a high contact angle, and C has a small contact angle.

Examples: drops of oil, water and water + detergent

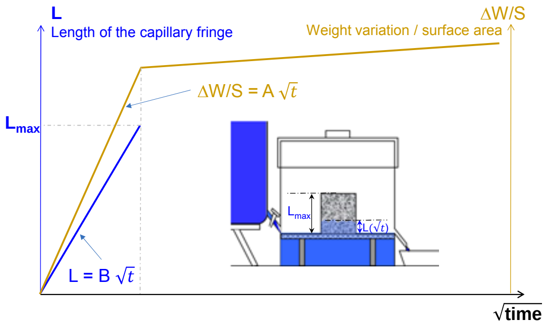
Liquid water in porous media – surface tension

For example, inorganic salts (in general!) increase the surface tension (decrease the wettability) of a solution, but alcohols or surfactants decrease the surface tension (increase the wettability) of the solutions

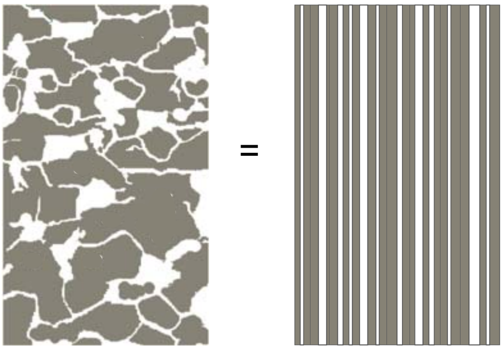
Some treatment effects:
Hydrophobic and consolidating treatments decrease the wettability of the façade surfaces whereas cleaning products tend to increase this wettability

Liquid water in porous media – capillarity

capillary imbibition : kinetics

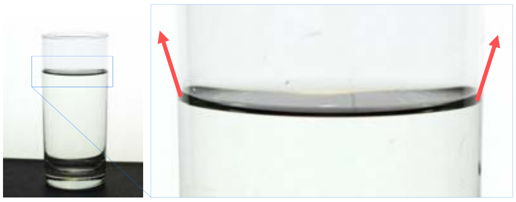


Capillary water in porous media – model

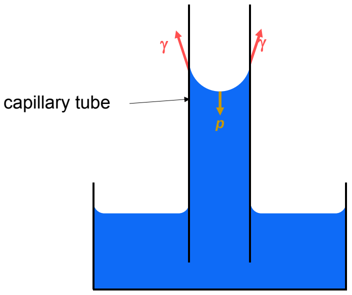


Liquid water in porous media – surface tension :

hydrophilic solid + liquid water =>
spontaneous formation of menisci

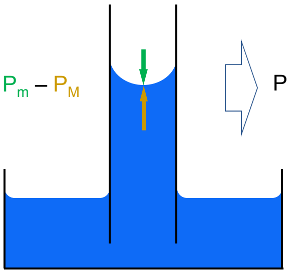


Capillary water in porous media – model



Capillary water in porous media – model

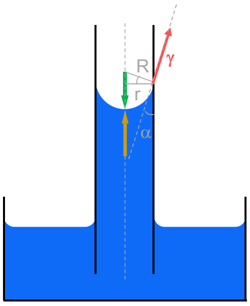
Capillary pressure (Pc) =
pressure in the less wetting fluid (P_m) – pressure in the more wetting fluid (P_M)



Pc = $P_m - P_M$

Pc = $P_{air} - P_{water}$

Capillary water in porous media – model



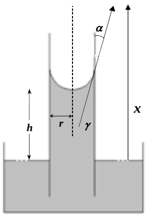
Relation between Pc and the capillary radius
(Laplace equation)

Pc = 2 γ / R

Pc = capillairy pressure
γ = surface tension liquid/gas
R = radius of curvature of the menisc

if **r** (capillary radius) is very small
=> **Pc = 2 γ cosα / r**

Capillary water in porous media – model



When a capillary tube is plunged in a liquid, the meniscus moves allong the tube.

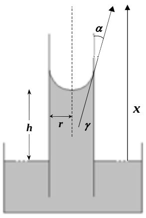
The kinetic follows the **Poiseuille law** which is (if acceleration due to gravity is neglected) :

$$Q\ (x) = \frac{\pi\ \gamma\ \cos\alpha\ r^3}{4\ \eta\ x}$$

=> when r ↗, Q ↗

γ = surface tension liquid/gas
r = radius of the capillary
η = dynamic viscosity
α = contact angle solid/liquid

Capillary water in porous media – model



When a capillary tube is plunged in a liquid, the meniscus moves allong the tube.

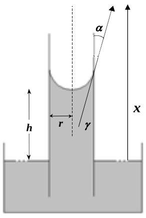
The height *h* of the liquid column at stady state is given by the Jurin's equation :

$$h = \frac{2\ \gamma\ \cos\alpha}{r\ g\ \rho}$$

=> when r ↗, h ↘

γ = surface tension liquid/gas
g = gravitiy
ρ = density of liquid
r = radius of the capillary
α = contact angle solid/liquid

Calculation examples



For a water-filled glass tube in air at sea level,

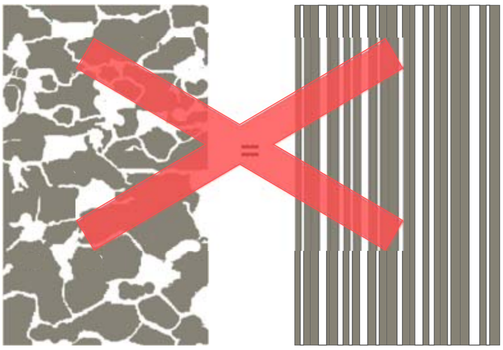
γ = 0.0728 J/m² at 20°C
θ = 20° (0.35 rad)
ρ = 1000 kg/m^3
g = 9.8 m/s²

=> the height of the water column is given by:

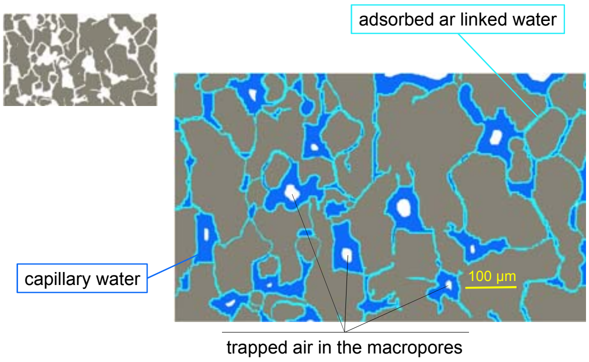
$$h = \frac{2\ \gamma\ \cos\alpha}{r\ g\ \rho} \approx \frac{1.4 \times 10^{-5}}{r}$$

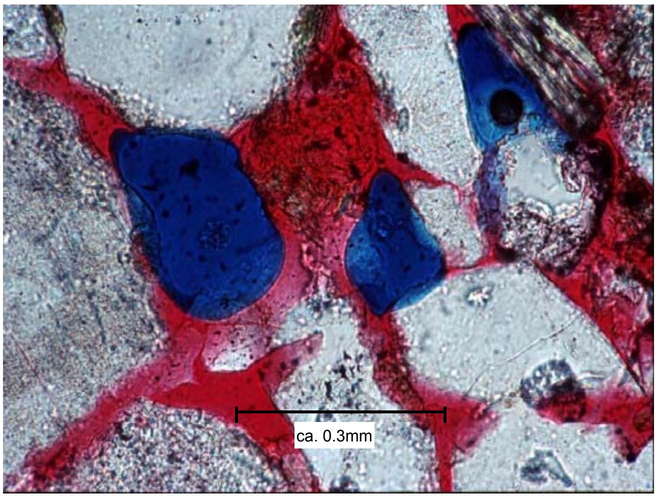
Thus for a 2 m wide (r = 1 m) tube, the water would rise an unnoticeable 0.014 mm.
For a 2 cm wide tube (r = 1 cm), the water would rise 1.4 mm
and for a capillary tube with r = 0.1 mm, the water would rise 14 cm.

Capillary water in porous media – real life

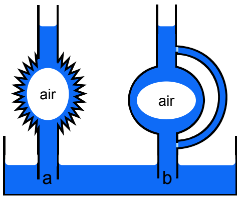


Liquid water in porous media – capillarity





Liquid water in porous media – capillarity

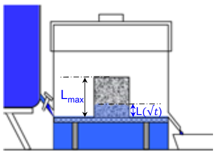


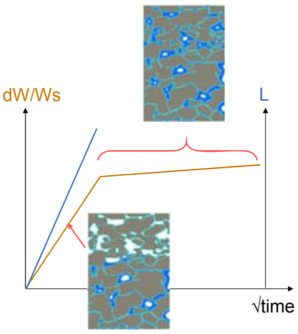
Less wetting fluid trapped by the more wetting fluid during an imbibition because of:
a. rugosity
b. derivation

The porosity of a rock (or a mortar, a concrete,…) is a complex system formed by inter-connected wide and tiny pores. As a result, there are always many parallel ways for the capillary water during an **imbibition**.
This great complexity allows the water (more wetting fluid) to trap air (less wetting fluid) in parts of the porosity.

Liquid water in porous media – capillarity

Capillary imbibition





Liquid water in porous media – capillarity

During a **capillary imbibition**:

Porosity freely accessible to water = **free porosity**
Portion of porous space inaccessible = **trapped porosity**

The trapped porosity is caracterised by the capillary saturation coefficient or **Hirschwald coefficient (S%)**

$$S\% = \frac{P_i}{Pt} \times 100 \quad \text{where} \quad Pi\,(\%) = \frac{M_i - M_1}{M_2 - M_3} \times 100$$

P_i = porosity filled by water imbibition
M_i = sample weight after water imbibition
M_1, M_2, M_3: see page 15

Liquid water in porous media – gelivity

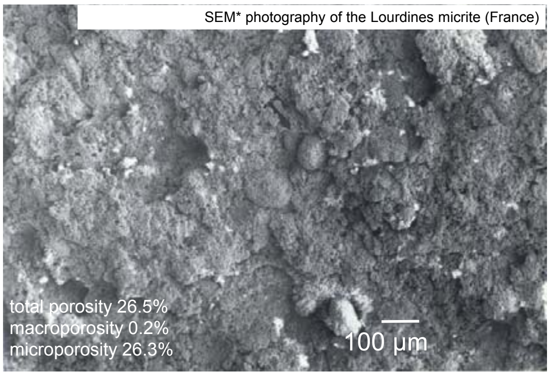
The ability to be more or less filled with water in the presence of air **is one of the lot of parameters** controling the frost resistance of a stone

Estimation of frost resistance :

In a “simplistic” way, a stone is described as
- **frost susceptible** if S% is > 0,85
- **not frost susceptible** if S% is < 0,75

A high water saturation makes the stone frost susceptible (because of the volume expansion of about 9% - or a linear expansion of 3% - of this liquid when it freezes)

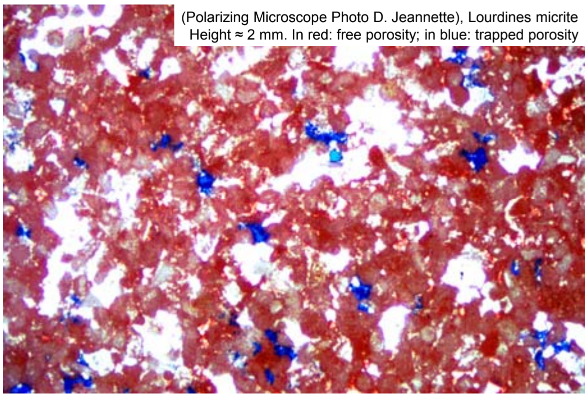
SEM* photography of the Lourdines micrite (France)

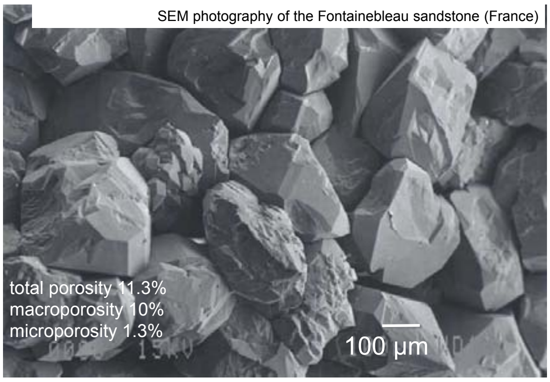


micro- < r = 7.5 µm < macro-porosity (p.11)

*SEM: Scanning Electron Microscope

(Polarizing Microscope Photo D. Jeannette), Lourdines micrite
Height ≈ 2 mm. In red: free porosity; in blue: trapped porosity

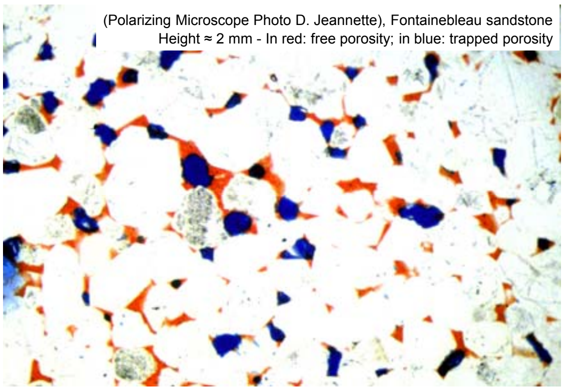




SEM photography of the Fontainebleau sandstone (France)

total porosity 11.3%
macroporosity 10%
microporosity 1.3%

micro- < r = 7.5 µm < macro-porosity (p.11)



(Polarizing Microscope Photo D. Jeannette), Fontainebleau sandstone
Height ≈ 2 mm - In red: free porosity; in blue: trapped porosity

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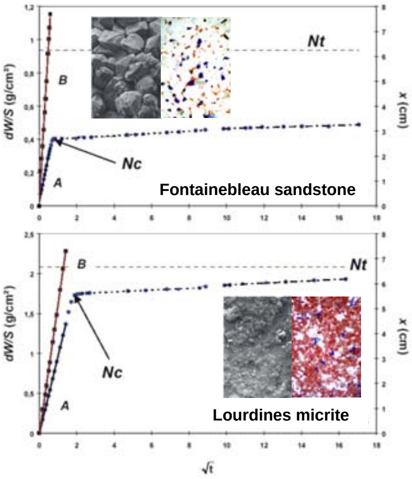
Capillary imbibition
(RH 100%, T 23° C)

dW = weight variation

S = imbibition surface

Nc = capillary porosity

Nt = total porosity



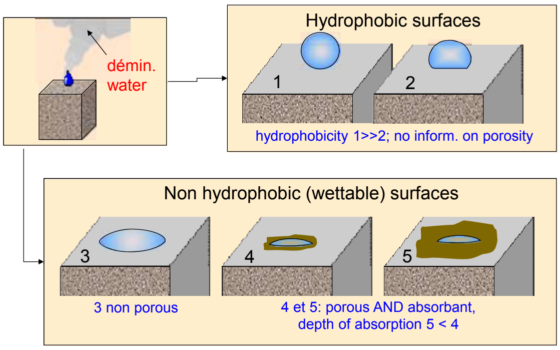
Liquid water in porous media – capillarity

- **In general**, the higher the dimension of the pores, the higher is the capillary imbibition velocity

- if the linear capillarity is much faster than the massic one, the trapped porosity is high => even if water goes up high, the water saturation of the porosity remains low

- the more varied the pore sizes, the bigger is the trapped porosity: media with very homogeneous porosity can reach very high water saturation of the porosity (at least near the water source)

The (field) drop test to estimate if a material is porous and/or hydrophobic and/or absorbant

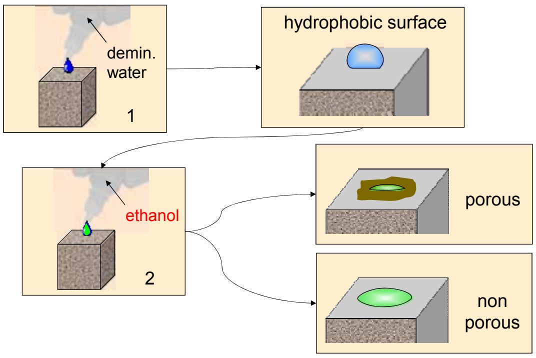


hydrophobicity 1>>2; no inform. on porosity

3 non porous

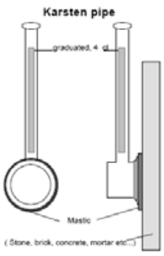
4 et 5: porous AND absorbant, depth of absorption 5 < 4

The (field) drop test to estimate if a material is porous and/or hydrophobic and/or absorbant



How to estimate the initial water absorption in the field: Karsten pipes

http://www.reedconstructiondata.com



Final Report for the Research and Development Project Non-Destructive Field Tests in Stone Conservation Literature Study Rapport från Riksantikvarieämbetet 2006:3 // http://www.raa.se/publicerat/9172094345.pdf

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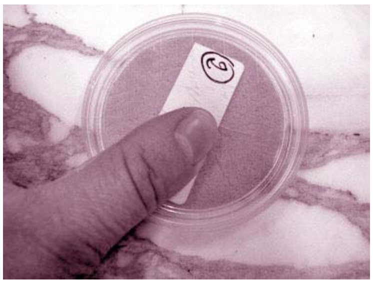
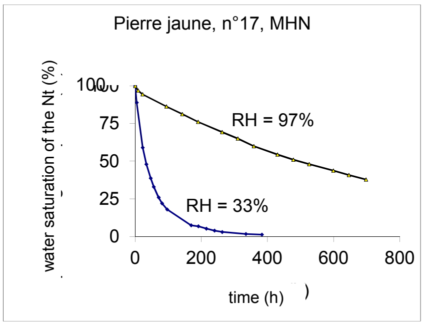
How to estimate the initial water absorption in the field: contact sponge

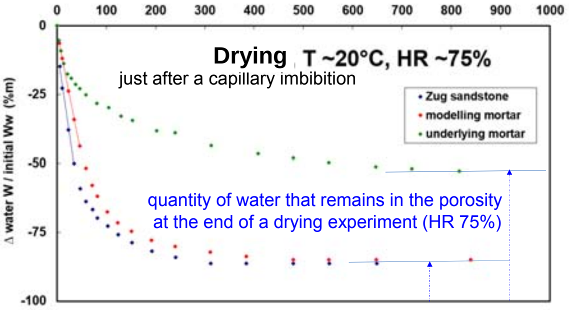


Marini P., Bellopede R., 2009- Bowing of marble slabs: Evolution and correlation with mechanical decay. Construction and Building Materials, Vol. 23, Issue 7, pp 2599–2605

Liquid water in porous media – drying



Liquid water in porous media – drying



Drying T ~20°C, HR ~75%

just after a capillary imbibition

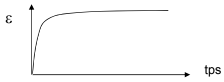
quantity of water that remains in the porosity at the end of a drying experiment (HR 75%)

Liquid water in porous media – dilation (dilatation)

Every porous material changes more or less its dimensions when it adsorbs (vapor) or absorbs (liquid) water (because of a loss of cohesion between grains and or the swelling of clays). This phenomenon is called **hydric dilation** (with liquid water) or **hygric dilation** (with water vapour).

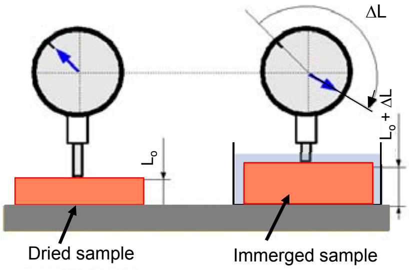
Hydric dilation measurement: the dried sample (length: L_0) is fixed under a dial test indicator *(comparateur)*, then it is entirely immersed in water. The extension which is obtained after 72 hours of immersion allows to calculate the hydric dilation coefficient:

$$\varepsilon(72) = \frac{\Delta L\ (72\ h)}{L_0}$$



$\varepsilon(72) \geq 2$ mm/m is regarded as high and dangerous

Liquid water in porous media – dilation (dilatation)



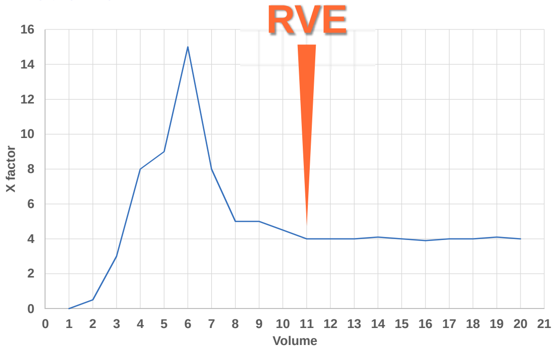
Notion of R.V.E.

Rocks are **heterogeneous materials** (mineralogy, porosity) on a scale of:

- **pores**
- **samples**
- **outcrops** *(affleurements)*

Therefore to be representative, measurements of physical and mechanical properties of rocks must be done on **Representative Volume Elements** *(volumes élémentaires représentatifs)*.

Notion of R.V.E.



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